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Etymology of math

The word mathematics comes from the Greek μάθημα (máthēma), which, in the ancient Greek language, means “what one learns”, “what one gets to know”, hence also “study” and “science”, and in modern Greek just “lesson”. The word máthēma is derived from μανθάνω (manthano), while the modern Greek equivalent is μαθαίνω (mathaino), both of which mean “to learn”. In Greece, the word for “mathematics” came to have the narrower and more technical meaning “mathematical study”, even in Classical times. Its adjective is μαθηματικός (mathēmatikós), meaning “related to learning” or “studious”, which likewise further came to mean “mathematical”. In particular, μαθηματικὴ τέχνη (mathēmatikḗ tékhnē), Latin: ars mathematica, meant “the mathematical art”. In Latin, and in English until around 1700, the term mathematics more commonly meant “astrology” (or sometimes “astronomy”) rather than “mathematics”; the meaning gradually changed to its present one from about 1500 to 1800. This has resulted in several mistranslations: a particularly notorious one is Saint Augustine's warning that Christians should beware of mathematici meaning astrologers, which is sometimes mistranslated as a condemnation of mathematicians. The apparent plural form in English, like the French plural form les mathématiques (and the less commonly used singular derivative la mathématique), goes back to the Latin neuter pluralmathematica (Cicero), based on the Greek plural τὰ μαθηματικά (ta mathēmatiká), used by Aristotle (384–322 BC), and meaning roughly “all things mathematical”; although it is plausible that English borrowed only the adjective mathematic(a) and formed the noun mathematics anew, after the pattern of physics and metaphysics, which were inherited from the Greek. In English, the noun mathematics takes singular verb forms. It is often shortened to maths or, in English-speaking North America, math. Definitions of mathematics
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Aristotle defined mathematics as “the science of quantity”, and this definition lasted until the 19th century. Starting in the 19th century when the study of hearing increased in rigor and began to focus on abstract topics such as projective geometry, which have no clear relation to quantity or measurement, mathematicians and philosophers began to propose a variety of new definitions. Some of these definitions emphasize the deductive character of much of mathematics, some emphasize its abstractness, some emphasize certain topics within mathematics. Today, no consensus on the definition of mathematics prevails, even among professionals. There is not even consensus on whether mathematics is an art or a science. A great many professional mathematicians take no interest in a definition of mathematics, or consider it undefinable. Some just say, “Mathematics is what mathematicians do.” Three leading types of definition of mathematics are called logicist, intuitionist, and formalist, each reflecting a different philosophical school of thought. All have severe problems, none has widespread acceptance, and no reconciliation seems possible. An early definition of mathematics in terms of logic was Benjamin Peirce’s “the science that draws necessary conclusions” (1870). In the Principia Mathematica, Bertrand Russell and Alfred North Whitehead advanced the philosophical program known as logicism, and attempted to prove that all mathematical concepts, statements, and principles can be defined and proven entirely in terms of symbolic logic. A logicist definition of mathematics is Russell’s “All Mathematics is Symbolic Logic” (1903). Intuitionist definitions, developing from the philosophy of mathematician L.E.J. Brouwer, identify mathematics with certain mental phenomena. An example of an intuitionist definition is “Mathematics is the mental activity which consists in carrying out constructs one after the other.” A peculiarity of intuitionism is that it rejects some mathematical ideas considered valid according to other definitions. In particular, while other philosophies of mathematics allow objects that can be proven to exist even though they cannot be constructed, intuitionism allows only mathematical objects that one can actually construct. Formalist definitions identify mathematics with its symbols and the rules for operating on them. Haskell Curry defined mathematics simply as “the science of formal systems”. A formal system is a set of symbols, or tokens, and some rules telling how the tokens may be combined into formulas. In formal systems, the word axiom has a special meaning, different from the ordinary meaning of “a self-evident truth”. In formal systems, an axiom is a combination of tokens that is included in a given formal system without needing to be derived using the rules of the system. “mathematical science,” late 14c, as singular noun, mathematik (replaced since early 17c. by mathematics, q.v.), from Old French mathematique and directly from Latin mathematica (plural), from Greek mathēmatikḗ tékhnē “mathematical science,” feminine singular of mathēmatikós (adj.) “relating to mathematics, scientific, astronomical; pertaining to learning, disposed to learn,” from mathēma (genitive mathēmatós) “science, knowledge, mathematical knowledge; a lesson,” literally “that which is learnt;” from manthanein “to learn,” from PIE root *mendh- “to learn.” As an adjective, “pertaining to mathematics,” from c. 1400, from French mathématique or directly from Latin mathematicus.American English shortening of mathematics, 1890; the British preference, maths, is attested from 1911. “Math. is used as an abbreviation in written English in the U.K. but not in speech, the normal form being Maths” [OED].maths=metamathematics=ics=mendh=See All Related Words (6)Advertisementadapted from books.google.com/ngrams/ with a 7-year moving average; ngrams are probably unreliable.c. 1300, philosophie, “knowledge, learning, scholarship, scholarly works, body of knowledge,” from Old French filosofie “philosophy, knowledge” (12c., Modern French philosophie) and directly from Latin philosophia, from Greek philosophia “love of knowledge, pursuit of wisdom; sys “the science of quantity; the abstract science which investigates the concepts of numerical and spatial relations,” 1580s; see mathematic (the older form of the word in English, attested from late 14c.). + -ics. Originally one of three branches of Aristotelian theoretical science, along with first philosophy (or metaphysics) and physics (or natural philosophy). Mystical doctrines as to the relation of time to eternity are also reinforced by pure mathematics, for mathematical objects, such as numbers, if real at all, are eternal and not in time. Such eternal objects can be conceived as God’s thoughts. (Bertrand Russell, “A History of Western Philosophy”) “of pertaining to, or of the nature of mathematics,” early 15c., from Medieval Latin mathematicus “of or belonging to mathematics,” from Latin mathematicus (see mathematic) (1). Also, by 1765, “pertaining to the quadrivium,” comprising arithmetic, geometry, astronomy, and music. It also could include optics. Related: Mathematically. The four mathematical arts are arithmetic, geometry, music, and astronomy; these anciently were termed the quadrivium, or fourfold way of knowledge. [Sir John Hawkins, “A General History of the Science and Practice of Music.” Sir John Hawkins, 1776] Mathematics is a tricky subject for some students. Some brains are wired for math, and some brains are wired for the humanities. Or should I say, some brains are wired for ‘maths’, and some are wired for the humanities? You see, as tricky as math (or ‘maths’) can be, the gift of a linguist is to be able to take any simple, straight-forward subject, and make it needlessly complicated. You see, in North America when we discuss mathematics, we use the abbreviation math. Though UK English speakers choose to abbreviate the singular mathematic and then pluralize that abbreviation to maths. British English speakers will often tease Americans for our misuse of the language that they invented. But according to the Online Etymology Dictionary, the American shortening of mathematics dates back to 1890, while “the British preference, maths, is attested from 1911.” It would seem then that the word was corrupted in the opposite direction over the Atlantic! But other attestations confuse the matter further. For example Lewis Carroll, the writer of Alice in Wonderland and professional mathematician, used the abbreviation math twice in a diary entry from March 29th, 1885: A book of Math. curiosities, which I think of calling ‘Pillow Problems, and other Math. Trifles.’ This will contain Problems worked out in the dark, Logarithms without Tables, Sines and angles do, a paper I am now writing on ‘Infinities and Infinitesimals,’ condensed Log Multiplication, and perhaps others. Carroll’s diary entry comes 5 years before the Online Etymology Dictionary’s first attestation of ‘math’. And interestingly enough, it occurs in England by an Englishman. And yet, even earlier than Carroll’s use of math, American examples of maths have appeared in print. Throughout the 1860s, a series of ads in The American Educator monthly began committing to the abbreviation maths. At West Point manual entitled Regulations of the US Military Academy, at West Point also used the abbreviation maths. Though the examples above, maths are used as shorter versions of the word mathematics in publications where space is limited. Notice how each example includes a period after the abbreviation? And in the example from West Point, maths only appears in a table where mathematics will not fit. Elsewhere in the table (and throughout the rest of the manual), the writer favors the term mathematics. Which brings up an important question. Since people often improve abbreviations on an ‘as needed’ basis, when does an abbreviation gain enough acceptance to become a word in its own right? Surely in the millennia long history of the word mathematics and its ancestors (mathematice in Old French, mathematica in Latin, mathēmatikḗ tékhnē in Ancient Greek), countless people must have started writing the word mathematics, run out of room on the page, and just stopped at any random point. M, mathe, mthmcs, math and Maths are all valid abbreviations depending on the context. But Math and Maths are not just abbreviations. They’ve become words in their own right. It’s perfectly natural for a person to say, ‘I teach math.’ But no one would say, ‘I teach Eng.’ Neither math nor maths are simply abbreviations. They are words. This puts math and maths in a pretty special category of word. They’re not acronyms which shorten a series of words—like how laser means ‘light amplification by stimulated emission of radiation’. Nor are they a single word shortened phonetically—like donut for doughnut or thru for through. Math and maths began life as a longer word, became shortened and slowly began to replace their predecessor—like how telephone became phone or how advertisement became ad. Each version of the word does a little something different though. Math is a ‘shortening’ of mathematics, while maths is a ‘contraction’ of mathematics. The contraction benefits the reader by incorporating the plural word. But then again, mathematics is singular – its contraction (notice how I used the word is). So perhaps math is a better representation. In the King’s English (published in 1908), HW Fowler had nothing to say about math or maths. Perhaps they didn’t gain popularity until after his passing. But he had quite a bit to say about Americans. Though we take these separately from foreign words, the distinction is purely form. Americans are foreign words, and should be so treated. To say this is not to insult the American language. . . It must be admitted that they and we, in parting some hundreds of years ago, departed on slightly divergent roads in language long before we did so in politics. Regardless of who first used math or maths, regardless of who originated the language, it is clear American English and British English became different languages long ago. And so they will evolve in their own ways. Whether you use math, maths or mathematics, remember that English conforms to its users. And nothing in linguistics is as simple or straight-forward as math(s). Share – copy and redistribute the material in any medium or format for any purpose, even commercially. Adapt – remix, transform, and build upon the material for any purpose, even commercially. The licensor cannot revoke these freedoms as long as you follow the license terms. Attribution – You must give appropriate credit , provide a link to the license, and indicate if changes were made . You may do so in any reasonable manner, but not in any way that suggests the licensor endorses you or your use. ShareAlike – If you remix, transform, or build upon the material, you must distribute your contributions under the same license as the original. No additional restrictions – You may not apply legal terms or technological measures that legally restrict others from doing anything the license permits. You do not have to comply with the license for elements of the material in the public domain or where your use is permitted by an applicable exception or limitation . No warranties are given. The license may not give you all of the permissions necessary for your intended use. For example, other rights such as publicity, privacy, or moral rights may limit how you use the material. Area of knowledge “Math” and “Maths” redirect here. For other uses, see Mathematics (disambiguation) and Math (disambiguation). Part of the series on Mathematics history index: Areas Number theory Geometry Algebra Calculus and Analysis Probability Statistics and Decision Theory Physics Chemistry Geosciences Computation Biology Linguistics Philosophy Education Mathematics Portal Math is a field of study that discovers methods, theories and theorems that are developed and proved for the needs of empirical sciences and mathematics (see below). There are many areas of mathematics, which include number theory (the study of numbers), algebra (the study of formulas and related structures), geometry (the study of shapes and spaces that contain them), analysis (the study of continuous changes), and set theory (presently used as a foundation for all mathematics). Mathematics involves the description and manipulation of abstract objects that consist of either abstractions from nature or—in modern mathematics—purely abstract entities that are stipulated to have certain properties, called axioms. Mathematics uses pure reason to prove properties of objects, a proof consisting of a succession of applications of deductive rules to already established results. These results include previously proved theorems, axioms, and—in case of abstraction from nature—some basic properties that are considered true starting points of the theory under consideration.[1] Mathematics is essential in the natural sciences, engineering, medicine, finance, computer science, and the social sciences. Although mathematics is extensively used for modeling phenomena, the fundamental truths of mathematics are independent of any scientific experimentation. Some areas of mathematics, such as statistics and game theory, are developed in close correlation with their applications and are often grouped under applied mathematics. Other areas are developed independently from any application (and are therefore called pure mathematics) but often later find practical applications.[2][3] Historically, the concept of a proof and its associated mathematical rigour first appeared in Greek mathematics, most notably in Euclid’s Elements.[4] Since its beginning, mathematics was primarily divided into geometry and arithmetic (the manipulation of natural numbers and fractions), until the 16th and 17th centuries, when algebra] and infinitesimal calculus were introduced as new fields. Since the 19th century, most of the study of linear equations (presently linear algebra) and quadratic equations in a single unknown, which were called algebraic equations (a term which is rarely used, although it may be ambiguous). During the 19th century, mathemians began to use variables to represent intersecting lines, Affine spaces (postulates), or are part of the definition of the subject of study (axioms). 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